To better mimic the sampling process, a negative binomial error was added to 1 the abundance counts every time a sample was randomly drawn from the simulated assemblage 2 in the *BiogTest* randomization algorithm. The negative binomial distribution was used to generate 3 realistic heterogeneity that often results from spatial clustering of individuals and other small-scale 4 processes. In practice this implies that each sample is drawn from a slightly different vector of 5 abundance counts. An example for abundance-based data better illustrate this process. For better 6 reproducibility of this example, we have included the R code that generates it, but note that due to 7 the random nature of the process itself, application of the code will generate each time different 8 results. Let's have two samples with the following counts of observed species abundances. 9

```
> x <- data.frame(sample1 = c(5, 7, 1, 0, 1), sample2 = c(0, 10, 1, 2, 1))
> x
  sample1 sample2
        5
1
                 0
2
        7
                10
3
        1
                  1
4
        0
                 2
5
        1
                 1
>
```

The total number of individuals in each sample is 14 and 15 respectively. Now let's create a simulated assemblage with a log-normal distribution of species abundances from which to draw random samples:

```
> library(rareNMtests)
> SR <- do.call("rbind", apply(x, 2, chao1))</pre>
> mr <- match(max(SR[,2]), SR[,2])
> range.SR <- c(SR[mr, 4], SR[mr, 5])</pre>
> richness <- round(runif(1, range.SR[1], range.SR[2]))</pre>
> sdlog <- runif(1, 0.1, 3.5)
> com <- rlnorm(richness, 0, sdlog)</pre>
> com <- ceiling(com/min(com[com>0]))
> com
 [1]
      478
             36
                   12
                          9
                              27
                                    51
                                          47
                                               25
                                                     54
                                                           88
                                                                11
                                                                      22
                                                                            10
                                                                                164 1194
[16]
             19
                         43
                              67
                                     3
        16
                    1
                                          18
>
```

The algorithm will now extract two random samples (with replacement) of 14 and 15 individuals from this assemblage, respectively, with probability weights proportional to the abundance counts in the assemblage. The vector of probabilities is thus the result of adding a negative binomial error to the abundance count of each species in the assemblage (i.e. the expectation μ of the negative binomial). The variance of the negative binomial is:

$$var = \mu + \frac{\mu^2}{k}$$

where k is the dispersion parameter. For every species, k was randomly drawn from a uniform distribution between 0.01 and 25 each time a sample was drawn from the assemblage, as shown in the example below:

```
> prob1 <- rnbinom(n = length(com), mu=com, size=runif(length(com), 0.01, 25))</pre>
> prob1
                                                           9 186 394 11 21
                       25
                             0 37
                                    36
                                        77 61 11 19
 [1] 670
          22
                                                                                 2
                                                                                     44
                6
                   14
           4
[20]
      88
               28
> prob2 <- rnbinom(n = length(com), mu=com, size=runif(length(com), 0.01, 25))</pre>
> prob2
                                                        76
 [1]
      351
             51
                  12
                        17
                             31
                                   43
                                        41
                                             24
                                                   41
                                                              13
                                                                   38
                                                                          9
                                                                             228 1622
[16]
                   0
                       95
                             49
       14
             20
                                   0
                                        23
```

>

And now the assemblage is sampled using these vector of probabilities for each of the samples.

```
> sample1 <- sample(1:length(com), sum(x[,1]), replace=TRUE, prob=prob1)</pre>
> sample1 <- data.frame(table(sample1))</pre>
> colnames(sample1) <- c("species", "sample1")</pre>
> sample2 <- sample(1:length(com), sum(x[,2]), replace=TRUE, prob=prob2)</pre>
> sample2 <- data.frame(table(sample2))</pre>
> colnames(sample2) <- c("species", "sample2")</pre>
> df <- merge(sample1, sample2, by="species", all=TRUE)</pre>
> df[is.na(df)] <- 0
> df
  species sample1 sample2
1
         1
                  5
                           0
2
         8
                  1
                           0
         9
                  3
                           0
3
4
        15
                  4
                          11
5
       20
                  1
                           0
6
                  0
        14
                           1
```

>