

Appendix A

Brief Model Description of TRIPLEX-FLUX

TABLE A1. Variables and parameters used in TRIPLEX-FLUX for simulating old black spruce of boreal forest in Canada.

Symbol	Unit	Description	Equation and Value	Reference
A	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	net CO ₂ assimilation rate for big leaf	$A = \min(V_c, V_j) - R_d$ $A = g_s(C_a - C_i)/1.6$	Farquhar et al. (1980), Leuning (1990), Sellers et al. (1996)
A _{canopy}	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	net CO ₂ assimilation rate for canopy	$A_{\text{canopy}} = A_{\text{sun}}\text{LAI}_{\text{sun}} + A_{\text{shade}}\text{LAI}_{\text{shade}}$	Norman, (1982)
A _{shade}	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	net CO ₂ assimilation rate for shaded leaf		
A _{sun}	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	net CO ₂ assimilation rate for sunlit leaf		
Γ	Pa	CO ₂ compensation point without dark respiration	$\Gamma = 1.92 * 10^{-4} O_2^{1.75} (T-25)^{10}$	Collatz et al. (1991) and Sellers et al. (1992)
C _a	Pa	CO ₂ concentration in the atmosphere	Input variable	
C _i	Pa	Intercellular CO ₂ concentration		
f(N)	-	nitrogen limitation term	$f(N) = N/N_m = 0.8$	Bonan (1995)
f(T)	-	temperature limitation term	$f(T) = (1 + \exp((-220,000 + 710(T+273))/(R_{\text{gas}}(T+273))))^{-1}$	Bonan (1995)
g _s	$\text{m}\cdot\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	stomatal conductance	$g_s = g_o + m100A r_h / Ca$	Ball et al. (1988)
g _o	-	initial stomatal conductance	57.34	Cai and Dang (2002)
m	-	coefficient	Optimizable	7.43 by Cai and Dang (2002)
J	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	electron transport rate	$J = J_{\text{max}} \text{PPFD}/(\text{PPFD} + 2.1 J_{\text{max}})$	Farquhar and von Caemmerer (1982)
J _{max}	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	light-saturated rate of electron transport in the photosynthetic carbon reduction cycle in leaf cells	$J_{\text{max}} = 29.1 + 1.64 V_m$ Optimizable	Wullschleger (1993)
K	Pa	function of enzyme kinetics	$K = K_c (1 + O_2 / K_o)$	Collatz et al. (1991) and Sellers et al. (1992)
K _c	Pa	Michaelis–Menten constants for CO ₂	$K_c = 30 * 2.1 (T - 25)^{10}$	Collatz et al. (1991) and Sellers et al. (1992)
K _o	Pa	Michaelis–Menten constants for O ₂	$K_o = 30000 * 1.2 (T - 25)^{10}$	Collatz et al. (1991)

M	$\text{kg C}\cdot\text{m}^{-2}\cdot\text{day}^{-1}$	biomass density of each plant component	0.4 for leaf 0.28 for sapwood 1.4 for root	Gower et al. (1977) Kimball et al. (1997) Steel et al. (1997)
N	%	leaf nitrogen content	1.2	Based on Kimball et al. (1997)
N _m	%	maximum nitrogen content.	1.5	Bonan (1995)
O ₂	Pa	oxygen concentration in the atmosphere,	21,000	Chen et al. (1999)
PPFD	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	photosynthetic photon flux density	Input variable	
Q ₁₀	-	temperature sensitivity factor	Optimizable	2.0 by Goulden et al. (1998)
R _a	$\text{kg C}\cdot\text{m}^{-2}\cdot\text{day}^{-1}$	autotrophic respiration	$R_a = R_m + R_g$	
r _a	-	carbon allocation fraction	0.4 for root 0.6 for leaf and sapwood	Running and Coughlan (1988)
R _d	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	leaf dark respiration	$R_d = 0.015V_m$	Collatz et al. (1991)
R _e	$\text{kg C}\cdot\text{m}^{-2}\cdot\text{day}^{-1}$	ecosystem respiration	$R_e = R_a + R_h$	
R _g	$\text{kg C}\cdot\text{m}^{-2}\cdot\text{day}^{-1}$	growth respiration	$R_g = r_g r_a \text{ GPP}$	Ryan (1991)
r _g	-	growth respiration coefficient	0.25 for root, leaf and sapwood	Ryan (1991)
R _{gas}	$\text{m}^3\cdot\text{Pa}\cdot\text{mol}^{-1}\cdot\text{K}^{-1}$	molar gas constant	8.3143	Chen et al., 1999
r _h	%	relative humidity	Input variable	
R _h	$\text{kg C}\cdot\text{m}^{-2}\cdot\text{day}^{-1}$	heterotrophic respiration	$R_h = R_{10}Q_{10}^{(T_s-T_b)/10}$	van't Hoff, 1898
R _m	$\text{kg C}\cdot\text{m}^{-2}\cdot\text{day}^{-1}$	maintenance respiration	$R_m = M r_m Q_{10}^{(T-T_0)/10}$ $T_0=20^\circ\text{C}$	Running and Coughlan (1988), Ryan (1991)
r _m	-	maintenance respiration coefficient	0.002 at 20°C for leaf 0.001 at 20°C for stem 0.001 at 20°C for root	Kimball et al. (1997)
T	°C	air temperature	Input variable	
V _c	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	Rubisco-limited gross photosynthesis rates	$V_c = V_m (C_i - \Gamma)/(C_i - K)$	Farquhar et al. (1980)
V _j	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	Light-limited gross photosynthesis rates	$V_j = J (C_i - \Gamma)/(4.5C_i + 10.5\Gamma)$	Farquhar and von Caemmerer (1982)
V _{max}	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	maximum carboxylation rate	$V_{\text{max}} = V_{m25}0.24(T - 25)f_{(T)}f_{(N)}$ Optimizable	Bonan (1995)
V _{m25}	$\mu\text{mol}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$	V _m at 25°C, variable depending on vegetation type	Included in optimized V _{max}	45 by Cai and Dang (2002)

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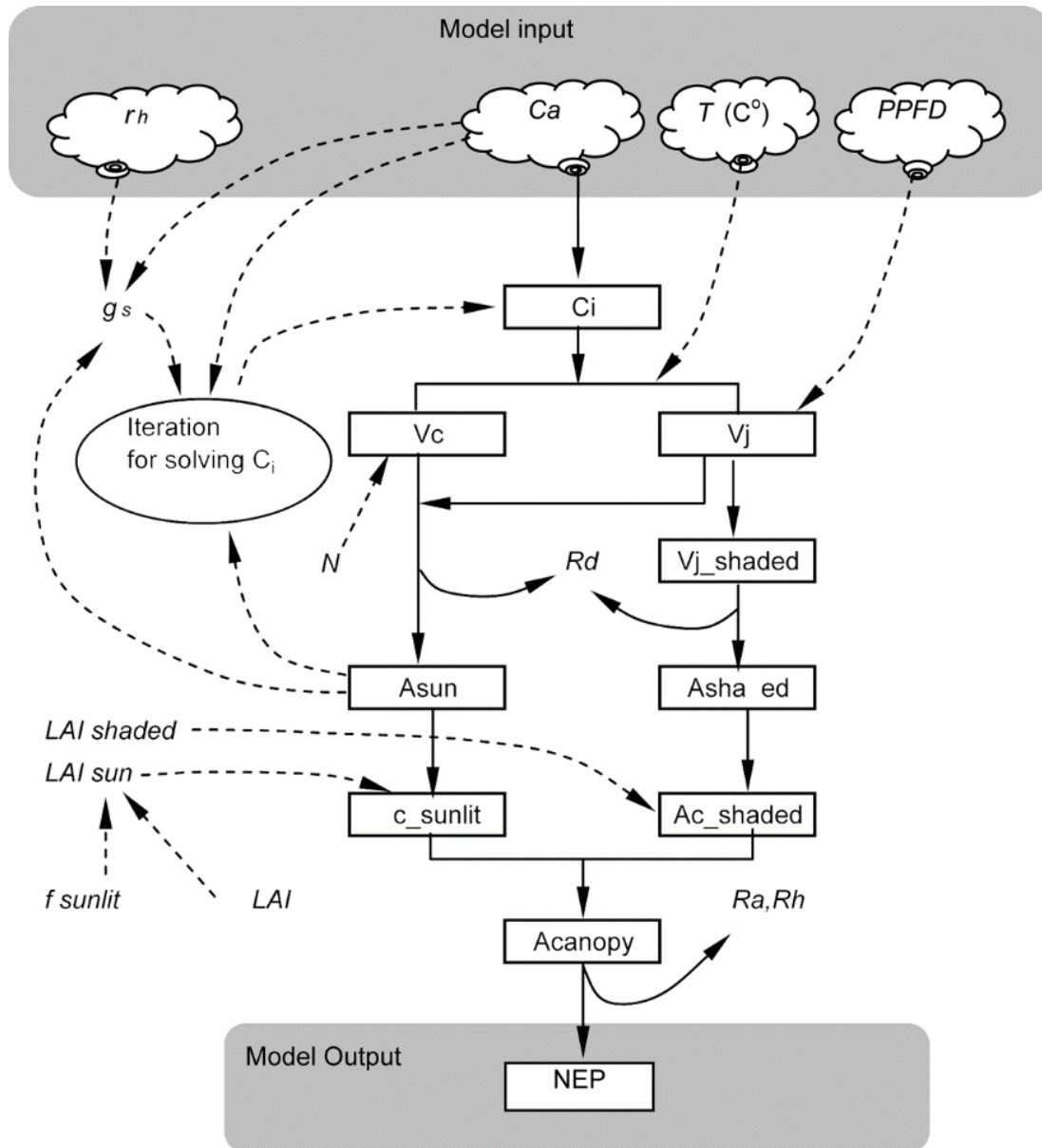


FIG. A1. The model structure diagram of TRIPLEX-FLUX. Solid lines represent carbon flows and the fluxes between the forest ecosystem and external environment; dashed lines denote control and effects of environmental variables; rectangles express state variables; the ellipse is a process of iteration. All symbols are expressed in Table A1.