

Appendix B

As a property of the definition of covariance $\sigma(aX, bY) = ab \sigma(x, y)$ and $\sigma(x + a, y) = \sigma(x, y)$, where a and b are constants,

$S_{12 \text{ within}}$ refers to selection differentials estimated from within treatment standardized trait (z) values and within treatment relative fitness (w) values.

Therefore,

$$1) S_{12 \text{ within}} = \sigma \left(\left(\frac{z - \bar{z}_{12}}{\sigma_{12}} \right), \frac{w}{\bar{W}_{12}} \right)$$

where z and w are individual trait and fitness values respectively; \bar{z}_{12} is the mean trait z in treatment 12, where both interacting species are present; σ_{12} is the standard deviation of trait z in treatment 12, and \bar{W}_{12} is the mean fitness (w) in treatment 12.

$$2) \sigma \left\{ \left(\frac{z - \bar{z}_{12}}{\sigma_{12}} \right), \frac{w}{\bar{W}_{12}} \right\} = \sigma \left\{ \left(\frac{z}{\sigma_{12}} - \left(\frac{\bar{z}_{12}}{\sigma_{12}} \right) \right), \frac{w}{\bar{W}_{12}} \right\}$$

\bar{z}_{12} , σ_{12} , and \bar{W}_{12} are effectively constants. Therefore,

$$3) \sigma \left\{ \left(\frac{z}{\sigma_{12}} - \left(\frac{\bar{z}_{12}}{\sigma_{12}} \right) \right), \frac{w}{\bar{W}_{12}} \right\} = \left(\frac{1}{\sigma_{12}} \right) \left(\frac{1}{\bar{W}_{12}} \right) \sigma(z, w)$$

Similarly, $S_{12 \text{ across}}$ refers to selection differentials estimated from trait values and fitness that have been standardized and relativized across all treatments. Therefore,

$$4) S_{12 \text{ across}} = \sigma \left\{ \left(\frac{z - \bar{z}}{\sigma_z} \right), \frac{w}{\bar{W}} \right\}$$

Where z and w are individual trait values and fitnesses in treatment 12 as in 1) above; \bar{z} is the grand mean trait value averaged across all individuals in the experiment; σ_z is the standard deviation of trait z across the entire experiment, and \bar{W} is the grand mean fitness averaged across all individuals in the experiment.

$$5) \sigma \left\{ \left(\frac{z - \bar{z}}{\sigma_z} \right), \frac{w}{\bar{W}} \right\} = \sigma \left\{ \left(\frac{z}{\sigma_z} - \frac{\bar{z}}{\sigma_z} \right), \frac{w}{\bar{W}} \right\}$$

\bar{z} , σ_z , and \bar{W} are effectively constants. Therefore:

$$6) \sigma \left\{ \left(\frac{z}{\sigma_z} - \frac{\bar{z}}{\sigma_z} \right), \frac{w}{\bar{W}} \right\} = \left(\frac{1}{\sigma_z} \right) \left(\frac{1}{\bar{W}} \right) \sigma(z, w)$$

Equations 3 and 6 can now be used to convert $S_{12 \text{ across}}$ into the more conventional $S_{12 \text{ within}}$

$$S_{12 \text{ within}} = \left(\frac{1}{\sigma_{12}} \right) \left(\frac{1}{\bar{W}_{12}} \right) \sigma(z, w) \text{ and } S_{12 \text{ across}} = \left(\frac{1}{\sigma_z} \right) \left(\frac{1}{\bar{W}} \right) \sigma(z, w)$$

$$\text{Therefore, } S_{12 \text{ within}} = \left(\frac{1}{\sigma_{12}} \right) \left(\frac{1}{\bar{W}_{12}} \right) * S_{12 \text{ across}} \bar{W} = \left(\frac{\sigma_z}{\sigma_{12}} \right) \left(\frac{\bar{W}}{\bar{W}_{12}} \right) S_{12 \text{ across}}$$

In cases where trait distributions are equal across treatments:

$$S_{12 \text{ within}} = \left(\frac{\bar{W}}{\bar{W}_{12}} \right) S_{12 \text{ across}}$$