

# Stilianos Louca and Michael Doebeli. 2015. Detecting cyclicity in ecological time series. *Ecology* 96:1724–1732.

## E LGSS models

For the simulations of the LGSS models we used an explicit two-step Runge-Kutta scheme, described in detail by Milstein (1995, §3.4, Theorem 3.3) and implemented in C++. Our source code is given as a separate supplement. The carrying capacity  $K$  and the intrinsic growth rate  $r$  were both normalized to 1, hence characteristic population sizes and time units are both 1. The standard deviation  $\sigma$  and the ratio  $\varepsilon/\sigma$  were randomly and uniformly chosen within the intervals  $[0.01, 0.2]$  and  $[0, 2]$ , respectively. For the cyclic model, the ratio  $\alpha/\sigma$  and the oscillation amplitude  $T$  were chosen uniformly within  $[1, 3]$  and  $[0.5, 4]$ , respectively. The amplitude  $A$  was calculated from the chosen  $\alpha$  and  $T$  using

$$A = \frac{\alpha}{r} \sqrt{r^2 + (2\pi/T)^2}. \quad (\text{E.1})$$

Cases for which  $A \geq K$  were skipped. Simulations ran for 25 time units and time series comprised 50 points. The integration time step was  $\delta t = 0.0002$ . We generated  $10^4$  independent time series for the non-cyclic as well as the cyclic model. Initial population sizes were chosen randomly according to the theoretical stationary distribution in the small-noise limit (i.e. as Gaussian variables with variance  $\sigma^2$  around the deterministic trajectory). Periodograms were analyzed as described in Band OUSS FAPs were corrected as described in C.

## LITERATURE CITED

Milstein, G. 1995. Numerical Integration of Stochastic Differential Equations. Mathematics and its Applications, Kluwer, Dordrecht, The Netherlands.