

Ecological Archives A017-091-A4

E. E. Holmes, L. W. Fritz, A. E. York, and K. Sweeney. 2007. Age-structured modeling reveals long-term declines in the natality of western Steller sea lions. *Ecological Applications* 17:2214-2232.

Appendix D. Parameter estimates and AIC_c values for model fits. [Table D1](#) shows scaling parameters and [Table D2](#) shows constants and variances.

Table D1. Maximum-likelihood estimates of the historical survivorship and birth rate relative to pre-decline levels. The models analyze the period 1976 to 2005. Vital rates are allowed to change as follows. The pre-decline period with vital rates fixed at pre-decline estimate is 1976 to 1982. Next come a series of time periods during which the vital rates are allowed to scale independently to a new value for the entire time period. The first time period, t_1 to (t_2-1) , is the same across all models: 1983 to 1987. The second time period is varied across models: 1988 to (t_3-1) . The third time period also varies across models: t_3 to (t_4-1) . If present in the model, the fourth time period is t_4 to (t_5-1) . The first column gives the $t_1, t_2, t_3, t_4,$ and t_5 values that define the time periods. The Leslie matrix used in the model is given in the second column (The Leslie matrices are described in [Appendix C](#)). The number of free parameters, K in the fourth column, is the number of scaling factors, 3, times the number of time periods, 3 to 4, plus 3 constants, $p_1, p_2, p_3,$ and the 3 variances in the likelihood function. The remaining columns show the scaling factors for the vital rates in each time period. $p_{j,k}$ is the scaling factor for juvenile survivorship in time period k . Juvenile survivorship in time period k is (pre-decline juvenile survivorship) $\times p_{j,k}$. $p_{a,k}$ is the scaling factor for adult survivorship in time period k . $p_{f,k}$ is the scaling factor for birth rate in time period k . The table is provided as a tab delimited text file in the [supplement](#). [Back to top](#)

| t_1, t_2, t_3, t_4, t_5 | Leslie matrix | ΔAIC_c | K | $p_{j,1}$ | $p_{j,2}$ | $p_{j,3}$ | $p_{j,4}$ | $p_{f,1}$ | $p_{f,2}$ | $p_{f,3}$ | $p_{f,4}$ | $p_{a,1}$ | $p_{a,2}$ | $p_{a,3}$ | $p_{a,4}$ |
|---------------------------|---------------|----------------|----|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 83 88 97 06 | HFYS | 5.454 | 15 | 0.436 | 0.877 | 1.241 | - | 0.908 | 0.841 | 0.813 | - | 0.879 | 0.921 | 0.963 | - |
| 83 88 97 06 | Y | 7.884 | 15 | 0.421 | 0.882 | 1.267 | - | 0.891 | 0.846 | 0.809 | - | 0.89 | 0.913 | 0.957 | - |
| 83 88 97 06 | CP | 15.133 | 15 | 0.443 | 0.93 | 1.311 | - | 0.924 | 0.873 | 0.83 | - | 0.872 | 0.892 | 0.952 | - |
| 83 88 97 06 | WT | 4.9 | 15 | 0.506 | 0.928 | 1.25 | - | 0.931 | 0.86 | 0.813 | - | 0.863 | 0.902 | 0.965 | - |

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|-----------------------|-------------|----------|-----------|-------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| 83 88 98 06 | HFYS | 7.148 | 15 | 0.43 | 0.911 | 1.241 | - | 0.903 | 0.839 | 0.787 | - | 0.881 | 0.918 | 0.981 | - |
| 83 88 98 06 | Y | 10.631 | 15 | 0.41 | 0.911 | 1.267 | - | 0.885 | 0.844 | 0.81 | - | 0.893 | 0.91 | 0.971 | - |
| 83 88 98 06 | CP | 17.332 | 15 | 0.442 | 0.998 | 1.311 | - | 0.929 | 0.902 | 0.84 | - | 0.869 | 0.882 | 0.963 | - |
| 83 88 98 06 | WT6 | 10.993 | 15 | 0.504 | 0.952 | 1.25 | - | 0.934 | 0.869 | 0.844 | - | 0.863 | 0.899 | 0.971 | - |
| 83 88 99 06 | HFYS | 12.193 | 15 | 0.39 | 0.901 | 1.241 | - | 0.897 | 0.829 | 0.813 | - | 0.885 | 0.925 | 0.996 | - |
| 83 88 99 06 | Y | 17.131 | 15 | 0.454 | 0.955 | 1.267 | - | 0.899 | 0.871 | 0.872 | - | 0.886 | 0.897 | 0.976 | - |
| 83 88 99 06 | CP | 22.312 | 15 | 0.393 | 0.991 | 1.311 | - | 0.913 | 0.872 | 0.879 | - | 0.878 | 0.888 | 0.974 | - |
| 83 88 99 06 | WT | 17.42 | 15 | 0.487 | 0.945 | 1.25 | - | 0.925 | 0.844 | 0.865 | - | 0.866 | 0.905 | 0.988 | - |
| 83 88 92 97 06 | HFYS | 0 | 18 | 0.42 | 0.734 | 0.565 | 0.935 | 0.869 | 0.762 | 0.703 | 0.641 | 0.899 | 0.928 | 1.002 | 1.068 |
| 83 88 92 97 06 | Y | 3.46 | 18 | 0.465 | 0.787 | 0.603 | 0.967 | 0.882 | 0.805 | 0.701 | 0.613 | 0.894 | 0.916 | 0.988 | 1.053 |
| 83 88 92 97 06 | CP | 6.385 | 18 | 0.481 | 0.818 | 0.621 | 0.998 | 0.903 | 0.827 | 0.725 | 0.628 | 0.882 | 0.889 | 0.965 | 1.029 |
| 83 88 92 97 06 | WT | 6.197 | 18 | 0.453 | 0.731 | 0.592 | 0.894 | 0.887 | 0.755 | 0.67 | 0.585 | 0.884 | 0.921 | 0.989 | 1.077 |
| 83 88 93 97 06 | HFYS | 7.341 | 18 | 0.42 | 0.739 | 0.591 | 0.986 | 0.871 | 0.754 | 0.724 | 0.657 | 0.898 | 0.934 | 1 | 1.053 |
| 83 88 93 97 06 | Y | 10.365 | 18 | 0.493 | 0.827 | 0.666 | 1.054 | 0.89 | 0.82 | 0.732 | 0.645 | 0.889 | 0.908 | 0.978 | 1.029 |
| 83 88 93 97 06 | CP | 14.262 | 18 | 0.506 | 0.85 | 0.675 | 1.08 | 0.91 | 0.834 | 0.754 | 0.657 | 0.877 | 0.887 | 0.961 | 1.013 |
| 83 88 93 97 06 | WT | 9.436 | 18 | 0.491 | 0.794 | 0.682 | 0.998 | 0.905 | 0.783 | 0.707 | 0.621 | 0.876 | 0.915 | 0.976 | 1.045 |
| 83 88 92 98 06 | HFYS | 4.161 | 18 | 0.42 | 0.74 | 0.622 | 0.974 | 0.871 | 0.761 | 0.7 | 0.646 | 0.899 | 0.929 | 0.998 | 1.075 |
| 83 88 92 98 06 | Y | 8.877 | 18 | 0.451 | 0.783 | 0.635 | 0.982 | 0.874 | 0.784 | 0.684 | 0.615 | 0.899 | 0.922 | 0.986 | 1.069 |
| 83 88 92 98 06 | CP | 9.504 | 18 | 0.428 | 0.772 | 0.611 | 0.968 | 0.882 | 0.78 | 0.69 | 0.608 | 0.893 | 0.901 | 0.969 | 1.056 |
| 83 88 92 98 06 | WT | 17.248 | 18 | 0.552 | 0.778 | 0.798 | 1.104 | 0.909 | 0.792 | 0.719 | 0.67 | 0.874 | 0.902 | 0.958 | 1.031 |
| 83 88 93 98 06 | HFYS | 10.82 | 18 | 0.395 | 0.712 | 0.627 | 0.966 | 0.864 | 0.738 | 0.708 | 0.647 | 0.902 | 0.941 | 1.006 | 1.075 |
| 83 88 93 98 06 | Y | 16.075 | 18 | 0.523 | 0.868 | 0.823 | 1.191 | 0.897 | 0.835 | 0.757 | 0.706 | 0.885 | 0.898 | 0.951 | 1.005 |
| 83 88 93 98 06 | CP | 17.738 | 18 | 0.479 | 0.828 | 0.716 | 1.085 | 0.896 | 0.801 | 0.727 | 0.649 | 0.885 | 0.893 | 0.959 | 1.03 |
| 83 88 93 98 06 | WT | 17.327 | 18 | 0.543 | 0.829 | 0.869 | 1.164 | 0.92 | 0.815 | 0.747 | 0.697 | 0.869 | 0.902 | 0.952 | 1.011 |
| 83 88 92 99 06 | HFYS | 12.072 | 18 | 0.433 | 0.731 | 0.678 | 1.034 | 0.868 | 0.757 | 0.694 | 0.668 | 0.898 | 0.927 | 0.998 | 1.075 |
| 83 88 92 99 06 | Y | 17.105 | 18 | 0.47 | 0.779 | 0.684 | 1.013 | 0.88 | 0.794 | 0.679 | 0.628 | 0.895 | 0.918 | 0.99 | 1.075 |
| 83 88 92 99 06 | CP | 16.272 | 18 | 0.378 | 0.695 | 0.578 | 0.897 | 0.871 | 0.753 | 0.653 | 0.593 | 0.9 | 0.911 | 0.987 | 1.081 |
| 83 88 92 99 06 | WT | 22.803 | 18 | 0.594 | 0.796 | 0.935 | 1.25 | 0.923 | 0.825 | 0.776 | 0.748 | 0.868 | 0.888 | 0.938 | 1.005 |

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|----------------|------|--------|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 83 88 93 99 06 | HFYS | 15.595 | 18 | 0.409 | 0.705 | 0.691 | 1.013 | 0.865 | 0.738 | 0.703 | 0.663 | 0.901 | 0.939 | 1.007 | 1.075 |
| 83 88 93 99 06 | Y | 20.396 | 18 | 0.55 | 0.867 | 0.937 | 1.266 | 0.909 | 0.86 | 0.792 | 0.752 | 0.879 | 0.89 | 0.939 | 0.992 |
| 83 88 93 99 06 | CP | 22.458 | 18 | 0.597 | 0.916 | 0.964 | 1.311 | 0.943 | 0.904 | 0.827 | 0.778 | 0.862 | 0.866 | 0.927 | 0.983 |
| 83 88 93 99 06 | WT | 21.272 | 18 | 0.574 | 0.828 | 0.964 | 1.25 | 0.93 | 0.838 | 0.786 | 0.746 | 0.865 | 0.894 | 0.942 | 1 |

Table D2. Maximum-likelihood estimates of the constants and variances for each model. p_1 translates to the expected average number of pre-decline female pups in the CGOA. p_2 is the scaling factor that translates the nonpup trend count into the total (unobserved) number of nonpup females in the population: $(1/p_2) \times \text{nonpup trend count} = \text{total number (unobserved) of nonpup females}$. p_3 is the scaling factor for the juvenile-fraction metric. See text for a full explanation of the constants. The model fit with lowest ΔAIC_c is shown in bold font.

The table is provided as a tab delimited text file in the [supplement](#). [Back to top](#)

| t_1, t_2, t_3, t_4, t_5 | Leslie matrix | ΔAIC_c | p_1 ÷1000 | p_2 | p_3 | σ^2 nonpup ×1000 | σ^2 pup ×1000 | σ^2 JT ×1000 |
|---------------------------|---------------|----------------------|----------------|-------|-------|----------------------------|-------------------------|------------------------|
| 83 88 97 06 | HFYS | 5.454 | 10.016 | 0.436 | 0.359 | 3.097 | 0.914 | 2.761 |
| 83 88 97 06 | Y | 7.884 | 10.004 | 0.453 | 0.368 | 3.121 | 0.892 | 3.555 |
| 83 88 97 06 | CP | 15.133 | 10.016 | 0.474 | 0.379 | 3.662 | 1.183 | 3.68 |
| 83 88 97 06 | WT | 4.9 | 10.029 | 0.424 | 0.37 | 3.659 | 0.794 | 2.521 |
| 83 88 98 06 | HFYS | 7.148 | 10.026 | 0.433 | 0.359 | 4.362 | 0.811 | 2.392 |
| 83 88 98 06 | Y | 10.631 | 10.013 | 0.454 | 0.369 | 4.744 | 0.749 | 3.254 |
| 83 88 98 06 | CP | 17.332 | 10.018 | 0.475 | 0.405 | 5.575 | 0.955 | 3.431 |
| 83 88 98 06 | WT | 10.993 | 9.996 | 0.429 | 0.377 | 5.66 | 0.873 | 2.227 |
| 83 88 99 06 | HFYS | 12.193 | 10.007 | 0.438 | 0.347 | 5.497 | 0.8 | 2.81 |
| 83 88 99 06 | Y | 17.131 | 10.000 | 0.458 | 0.396 | 6.719 | 0.847 | 3.15 |
| 83 88 99 06 | CP | 22.312 | 10.008 | 0.477 | 0.387 | 7.452 | 0.891 | 4.023 |

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|-----------------------|-------------|----------|---------------|--------------|--------------|--------------|--------------|--------------|
| 83 88 99 06 | WT | 17.42 | 10.010 | 0.430 | 0.364 | 7.683 | 0.908 | 2.409 |
| 83 88 92 97 06 | HFYS | 0 | 10.021 | 0.435 | 0.229 | 2.403 | 0.934 | 0.527 |
| 83 88 92 97 06 | Y1994 | 3.46 | 10.022 | 0.449 | 0.253 | 2.426 | 1.195 | 0.501 |
| 83 88 92 97 06 | CP | 6.385 | 10.026 | 0.471 | 0.254 | 2.742 | 1.312 | 0.483 |
| 83 88 92 97 06 | WT | 6.197 | 10.024 | 0.427 | 0.22 | 2.762 | 1.148 | 0.571 |
| 83 88 93 97 06 | HFYS | 7.341 | 10.028 | 0.434 | 0.241 | 2.538 | 0.917 | 0.975 |
| 83 88 93 97 06 | Y | 10.365 | 10.036 | 0.447 | 0.287 | 2.534 | 1.178 | 0.901 |
| 83 88 93 97 06 | CP | 14.262 | 10.037 | 0.469 | 0.284 | 2.956 | 1.257 | 0.946 |
| 83 88 93 97 06 | WT | 9.436 | 10.035 | 0.423 | 0.259 | 2.77 | 0.992 | 0.937 |
| 83 88 92 98 06 | HFYS | 4.161 | 10.008 | 0.436 | 0.233 | 3.158 | 0.883 | 0.576 |
| 83 88 92 98 06 | Y | 8.877 | 10.018 | 0.450 | 0.246 | 3.845 | 1.106 | 0.49 |
| 83 88 92 98 06 | CP | 9.504 | 10.021 | 0.473 | 0.224 | 4.279 | 1.062 | 0.475 |
| 83 88 92 98 06 | WT | 17.248 | 10.030 | 0.423 | 0.282 | 3.175 | 1.002 | 1.56 |
| 83 88 93 98 06 | HFYS | 10.82 | 10.017 | 0.436 | 0.227 | 3.132 | 0.912 | 1.019 |
| 83 88 93 98 06 | Y | 16.075 | 10.035 | 0.445 | 0.331 | 3.359 | 0.938 | 1.425 |
| 83 88 93 98 06 | CP | 17.738 | 10.033 | 0.469 | 0.269 | 4.164 | 1.088 | 1.001 |
| 83 88 93 98 06 | WT | 17.327 | 10.037 | 0.421 | 0.31 | 3.051 | 0.971 | 1.729 |
| 83 88 92 99 06 | HFYS | 12.072 | 10.038 | 0.433 | 0.242 | 3.219 | 0.935 | 1.048 |
| 83 88 92 99 06 | Y | 17.105 | 10.025 | 0.448 | 0.255 | 3.489 | 1.527 | 0.737 |
| 83 88 92 99 06 | CP | 16.272 | 10.016 | 0.474 | 0.194 | 3.712 | 1.418 | 0.702 |
| 83 88 92 99 06 | WT | 22.803 | 10.027 | 0.421 | 0.328 | 3.125 | 0.949 | 2.852 |
| 83 88 93 99 06 | HFYS | 15.595 | 10.026 | 0.434 | 0.237 | 2.813 | 1.026 | 1.543 |
| 83 88 93 99 06 | Y | 20.396 | 10.023 | 0.446 | 0.364 | 2.976 | 0.999 | 2.287 |
| 83 88 93 99 06 | CP | 22.458 | 10.005 | 0.469 | 0.377 | 3.006 | 1.215 | 2.074 |
| 83 88 93 99 06 | WT | 21.272 | 10.027 | 0.421 | 0.338 | 2.849 | 0.972 | 2.724 |